

# Wheldrake with Thorganby CE Primary School

# **Mathematics Calculation Policy**

Working together to be the best we can be

This policy has been largely adapted from the White Rose Maths Hub Calculation Policy with further material added. It is a working document and will be revised and amended as necessary.



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
DDITION			
Early Years / Year 1 Combining two parts to make a whole: Doart- whole model. Joining two groups and then recounting all objects using one-to-one correspondence is a part, is a part and the whole is	Use a range of resources - teddy bears, shells, cars	s s s s s s s s s s s s s s s s s s s	Practice number formation eg 5 Mark marking to represent numbers eg IIIII or o o o o o 4 + 3 = 7 Four is a part, 3 is a part and the whole is seven. Use the part-part whole model to move to abstract 10 = 6 + 4
Starting at the bigger number and counting on The bigger number is To find the total, I need to start at the biggest number, then count on. (delete words as chn become more familiar)	Counting on using number lines using cubes	A bar model which encourages the children to count on, rather than count all.	The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? 4 + 2 5 + 12 = 17



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
First Then Now E.g. First there were 4 children on the bus, then 3 children got on, Now there are 7 children on the bus. (this will help with the inverse relationship and missing number)	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	First Then Now 4 $+3$ $74+3=74+3=74+3=75Start at the larger number on the number line and count on in ones or in one jump to find the answer.$	Place the larger number in your head and count on the smaller number to find your answer.
Making / regrouping to 10 (essential skill to support column addition later on) Children should be able to link addition to making 10 first and then adding remaining amount I need to make ten. I have left over. 10 + is	6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.	Children to draw the ten frame and counters/cubes.	7 + 4 = 7 + = 10 10 + = If I am at seven, how many more do I need to make 10. How many more do I need to add onto 10?

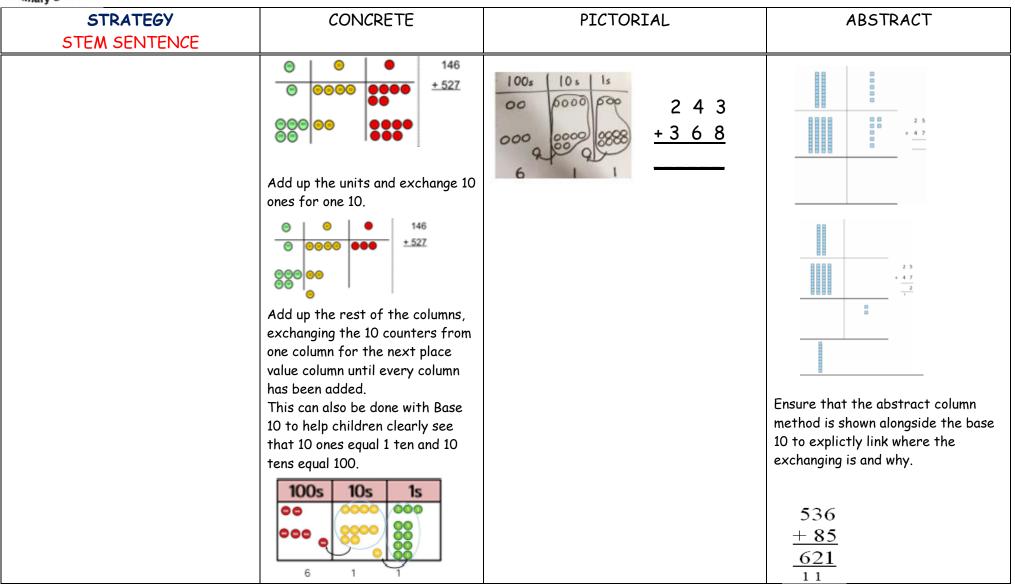


STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Adding three single digits Here the emphasis should be on the language rather than the strategy.	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7.		Combine the two numbers that make 10 and then add on the remainder. 4+7+6 = 10+7 = 17
and make ten Ten and is	As pupils are using the bead string, ensure that they are explaining using language such as; '1 more than 5 is equal to 6.' '2 more than 5 is 7.' '8 is 3 more than 5.'	Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Look for ways to make 10 and use this knowledge to solve, e.g. 9 + 3 + 4 = 10 + 2 + 4 = 16
<u>Year 2</u>	Use ten frame to make ten to	Use part part whole and number line to model	17 + 5 = 22
Add a two digit number and ones	start	17 + 5 = 22	Explore related facts 17 + 5 = 22
 and make (a multiple of ten).		$\begin{pmatrix} 3 \\ 16+7 \\ 16+7 \\ 16+7 \end{pmatrix}$	5 + 17 = 22
(Multiple of ten and (remainder) makes	Explore the pattern 17 + 5 = 22		22 - 17 = 5
e.g. 17 + 5	27 + 5 - 32	10 20 23	22 - 5 = 17
5 can be partitioned into 3 and 2. 17 and 3 make 20. 20 and 2 make 22.			22 17 5



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Column method - with grouping The is in the ones column, it represents one(s). The is in the tens column, it represents ten(s) Y2 to begin to use exchanging when ready	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions $\begin{array}{c c} T & 0 \\ \hline 0 & 0$	41 + 8 = 1 + 8 = 9 40 + 9 = 49 4 1 <u>+ 8</u> <u>4 9</u> double line is really important - equals sign
Year 3 Column method - with regrouping with up to 3 digits and carrying Year 2 only to two 2 digit numbers Year 3 onwards will work with larger numbers If the column sum is equal to ten or more, we must exchange We need to exchange ten ones for a ten	Make both numbers on a place value grid	Children to represent the base 10 in a place value chart.	Start by partitioning the numbers before moving on to clearly show the exchange below the addition. 20 + 5 <u>40 + 8</u> 60 + 13 = 73







STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
<u>Year 4</u> Column method- regrouping with up to 4 digits and carrying	As year 3 but with up to 4-digit numbers and with carrying	7       1       5       1	Th     H     T     O       2     6     3     4       +4     5     1     7       7     1     5     1       1     1     1
Year 5 and 6 Column method with regrouping. Dealing with larger numbers and decimals numbers. Children should also be able to solve inverse problems related to the column method.	As children move on to decimals. Money and decimal place value counters can be used to support	Use pictorial examples as year 4 if needed based on decimal values	As the children move on, introduce decimals with the same number of decimal places. Money can also be used here. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$



ABSTRACT
s 1s 0 2 ? 5 -



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
SUBTRACTION			
Early Years / Year 1	Use physical objects, counters, cubes etc to show how objects	First Then Now	4-3 =
Taking away ones	can be taken away.		= 4 - 3
When this is first			
introduced, the concrete representation should be based upon the diagram.	6 - 2 = 4	$4 - 1 \qquad 3 \qquad 4 - 1 = 3$	4
Real objects should be placed on top			3 ?
of the images as one - to - one correspondence so that pupils can take them away, progressing to	4 - 2 = 2	x x x x o	$\bigcirc$
representing the group of ten with a tens rod and ones with ones cubes	4 - 3 = 1		
First Then Now e.g. <b>First</b> there were 4 children in the	(double sided counters)	XXX	? 3
car, <b>then</b> 1 child got out, <b>Now</b> there are 3 children in the car.		Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.	
<u>Year 1</u>	Counting back (using number lines or number	Children to represent what they see pictorially e.g.	Children to represent the calculation on a number line or
Counting back	tracks) children start with 6 and count		number track and show their jumps. Encourage children to use
Subtracting 1, 2, or 3 by counting back.	back 2.		an empty number line
	6 - 2 = 4		



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Pupils should be encouraged to rely on number bonds knowledge as time goes on, rather than using counting back as their main strategy Start on and count back	1 = 2 = 4 $6 - 2 = 4$ Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. $13 - 4$ $Use  counters and move them away from the group as you take them away counting backwards as you go.$ $double  sided counters$	Represent what they see pictorially Count back on a number line or number track $0 \ 10 \ 11 \ 12 \ 13 \ 14 \ 15$ Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
<u>Year 2</u>			To progress to: Counting back in multiples in your
Counting back Subtracting by counting back.		34 35 36 374757This can progress all the way to counting back using two 2 digit numbers.	head, visualising the number line.



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STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Pupils should be encouraged to rely on number bonds knowledge as time goes on, rather than using counting back as their main strategy Start on and count back			
Make 10 As with addition, children see that it is more efficient to subtract to get to ten first then subtract again from ten. Knowledge of number bonds to and from ten and twenty are vital.		13 - 7 = 6 $3 4$ $3 4$ $-3$ To reach the next 10 I need to takeaway 3. 7 can be partitioned into 3 and 4. 13 takeaway 3 is ten. 10 takeaway 4 is 6.	16 - 8= How many do we take off to reach the next 10? How many do we have left to take off?
Part / Whole Model is the whole, is a part and is a part. First Then Now (as above)	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	10 - 5 = 5 10 Move to using numbers within the part whole model. 17 - 9 = 17 9



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STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Find the difference The difference is the amount between amounts.	S Pencils S Pencils	Count on to find the difference. +6 0 1 2 3 4 5 6 7 8 9 10 11 12 Draw bars to find the difference between 2 numbers. Comparison Bar Models Usa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 Usa Sister 22	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches. 23 - 15 = 8 Children to explore why 8-6 = 7-5 = 6-4
<u>Year 2 / 3</u>	Use Base 10 to make the bigger number then take the smaller	Draw the Base 10 or place value counters alongside the written calculation to help to	Start with expanded method to subtract
Column method without exchanging Subtract numbers with up to three digits, using formal written methods of columnar subtraction. The bigger number is so that goes at the top. Take away the, then takeaway the	number away Show how you partition numbers to	show working. $\begin{array}{c} \hline \\ \hline \\$	47 - 24 = 23 This will lead to a clear written column subtraction 4 8 - 7 4 1
	subtract. Make the larger number first		



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Year 2 / 3 / 4 Column method with regrouping Year 3 use 3digit numbers Year 4 onwards work with larger numbers	Lots of practical work with Base 10 deines at this stage Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions that exchange twice. $\boxed{05 \ 15} + \boxed{105 \ 15} + 105 \ 1$	Represent the place value counters pictorially; remembering to show what has been exchanged. $10s 1s$ $10s 1s$ $11s 1s 1s 1s$ $10s 1s$ $11s 1s 1s 1s$ $10s 1s$ $11s 1s 1s 1s$ $10s 1s 1s$ $11s 1s 1s 1s 1s$ $10s 1s 1s 1s$ $11s 1s 1s 1s 1s 1s 1s 1s 1s$ $10s 1s 1s$	Start formal written method by partitioning the number into clear place value columns $\boxed{836-254=582}\\\hline\frac{8}{360}+36-6\\\hline-200-50-4\\\hline\frac{3}{500-80-2}\\\hline\frac{200-50-4}{500-80-2}\\\hline\frac{200-50-4}{500-80-2}\\\hline\frac{200-50-4}{50-80-2}\\\hline\frac{200-50-40-50-4}{50-80-2}\\\hline200-50-50-40-50-50-50\\\hline\frac{200-50-50-50-50-$



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
	$\begin{array}{c c c c c c c c c c c c c c c c c c c $		
	I need to exchange one hundred for ten tens.		
	Image: Constraint of the constr		



STRATEGY STEM SENTENCE	CON	ICRETE	PICTORIAL	ABSTRACT
<u>Year 5 / 6</u> Column method		167-179 TO TO 167-179 TO TO 167-179 TO TO 167-179 TO TO 16 TO TO 16 TO 16 TO TO 16 TO 16 TO TO 16 TO 17 TO 16 TO 17 TO 16 TO 17 TO 16 TO 16 TO 16 TO 16 TO 16 TO T	As Year 4 but include decimal numbers	Move children onto using the column method to subract increasingly larger numbers. Including those where more than one borrow is required. $ \begin{array}{r}             4^3 & 9 & 13 \\             - & 2 & 8 & 4 \\             ====== \\             1 & 1 & 9 \end{array} $ Develp an understanding of subtracting any number including decimals. $ \begin{array}{r}             5 & 12 & 1 \\             - & 2 & 6 & .5 \\             2 & 3 & 6 & .5 \end{array} $



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
	Use concrete materials to represent columnal subtraction with decimal numbers.		
Conc	eptual variation; diff	erent ways to solve 391 -	186
<sup>391</sup> ? <sup>186</sup> 391 186 ?	Raj spent £391, Timmy spent £186. How much more did Raj spend? Calculate the difference between 391 and 186.	= 391 - 186 391 <u>-186</u>  What is 186 less than 391?	Missing digit calculations



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
MULTIPLICATION			
ГТ			

EYFS / Year 1	Use practical activities to	Draw pictures to show how to double a	Partition a number and then
Doubling Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. Doubling is an amount twice	show how to double a number double 4  is  8 $4 \times 2 = 8$ 1 + 1 = 12 1 + 1 = 12 1 + 1 = 12 1 + 1 = 12	Double 4 is 8	double each part before recombining it back together. 12 10 2 4 20 $420 + 4 = 24$
Counting in multiples We are counting in multiples of so we count every	Count in multiples supported by concrete objects in equal groups	$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} $	Count in multiples of a number aloud Write sentences with multiples of numbers 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Year 2         Repeated addition         There are in each group. There are groups. We have to add times.	There are 3 equal groups, with 4 in each group $3 \times 4$ 4 + 4 + 4 <b>Order 1</b> 3 + 3 + 3	<b>88</b> <b>88</b> <b>88</b> <b>88</b> <b>88</b> <b>88</b> <b>88</b> <b>88</b> <b>5</b> <b>5</b> <b>5</b> <b>5</b> <b>5</b> <b>5</b> <b>5</b> <b>5</b>	Write addition sentences to describe objects and pictures. $2 \times 5$ Abstract number line showing 3 groups of 4
Arrays- showing commutative multiplication lots of is the same as lots of	Create arrays using counters / cubes to multiplication sentences Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer	Draw arrays in different rotations to find commutative multiplication sentences. 4×2=8 2×4=8 00 4×2=8 00 00 00 00 00 00 00 00 00 00 00 00 00	Use an array to write multiplication sentences and reinforce repeated addition $10 = 2 \times 5$ $5 \times 2 = 10$ 2 + 2 + 2 + 2 + 2 = 10 10 = 5 + 5



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
<u>Year 2 / 3</u>	tens ones	24 × 3 =	4 × 15 =
Partition to multiply	× 3 7 2	10s 1s	partition
can be partitioned into and lots of ones is	<b>N V</b> .		4 × 10 = 40
lots of tens is ones add tens is			4 × 5 = 20
			recombine
		7 2	40 + 20 = 70
	25 x 4 =		4 × 15 = 70
<u>Year 3</u>	Show the link with arrays to first introduce the grid method.	Children can represent the work they have done with place value counters in a way	Start with multiplying by one digit numbers and showing the clear
Grid method	x 10 3 4 rows of 10	that they understand.	addition alongside the grid.
Recall and use multiplication and	<sup>4</sup> 4 rows	They can draw the counters, using colours	× 30 5
division facts for the 3, 4 and 8 multiplication tables.	of 3	to show different amounts or just use circles in the different columns to show	7 210 35
Write and calculate mathematical statements for multiplication and division using the multiplication tables	Move on to using Base 10 to move towards a more compact method.	their thinking	210 + 35 = 245



STRATEGY	CONCRETE	PICTORIAL		ABST	RACT	
STEM SENTENCE that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to	× т U 4 rows of 13	$\begin{array}{c c} 24 \times 3 = 72 \\ \hline \times 20 & 4 \\ \hline \end{array}$	Multiply b the differe method.			-
formal written methods. Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n	Move on to place value counters to show how we are finding groups of a number.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	× 10 4	<b>200</b> 2000 800	<b>30</b> 300 120	<b>2</b> 20 8
objects are connected to m objects.			200 80 30 120 2	0 0 0 0 0 <u>3</u>	+ 120 + 20	+ 8 =
Year 4 Column multiplication Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.	Formal column method with place value counters. 6 x 23	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods 23 x 6 =	leading to 3 2 7 <u>x 4</u> 2 8 8 0 <u>1 2 0 0</u> <u>1 3 0 8</u>	(7) (20) (300	< 4) < 4)	



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
We always need to start at the ones. ones times ones is ones. ones times tens is tens. Because we are multiplying by ten, we need to add in a zero as a place value holder. We cannot have more than one digit in any place value column, so we need to exchange ones as ten (and etc as needed)	100s       10s       1s         00       00       000         00       00       000         00       00       000         100s       10s       1s         000       000       000 <td><math display="block"> \begin{array}{c ccccccccccccccccccccccccccccccccccc</math></td> <td>1 leading to compact 3 2 7 <u>x 4</u> <u>1 3 0 8</u> 1 <del>2</del></td>	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 leading to compact 3 2 7 <u>x 4</u> <u>1 3 0 8</u> 1 <del>2</del>
Year 5 / 6 Column multiplication Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers.	Use all above strategies Children should be confident with using expanded notation to multiply	Use all above strategies Develop short method of multiplying with up to 4 digits by 1 or 2 digits including use of decimals 1342 x 18 13420 10736 24156	Show children the importance of lining up numbers including the decimal point. Talk about disregarding the decimal point and replacing it by however many decimal places if this is easier for children $\begin{array}{r} 2.43\\ x & 7\\ 17.01\\ 3 & 2 \end{array}$



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Conc	eptual variation: different	ways to ask children to solve	e 6 x 23
23 23 23 23 23 23 ?	Mai had to swim 23 lengths, 6 times a week. How many lengths did she swim in one week? With the counters, prove that 6 x 23 = 138	Find the product of 6 and 23 6 × 23 = ? ? = 6 × 23 23 6 <u>× 6</u> × 23 	What is the calculation? What is the product?



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STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
DIVISION			
<u>EYFS / Year 1</u> Sharing objects into groups		Children use pictures or shapes to share quantities.	Share 9 buns between 3 people. How many buns will each person get?
shared equally between is		<b>3 3 3 3 3 3 3 3 3 3</b>	9 ÷ 3 = 3
		12 ••• •• ••• 12 ÷ 4 = 3	
		Also use part-whole model	
Repeated subtraction We need to divide into groups of, so we need to take away each time. We have groups of	$6 \div 2 =$ $\begin{array}{c} & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ &$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Abstract number line to represent the equal groups that have been subtracted. $ \begin{array}{r} -2 & -2 & -2 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 \\ \hline 3 & groups \\ \end{array} $



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Year <u>2</u>	Divide quantities into equal groups.	Use a number line to show jumps in groups. The number of jumps equals the number	28 ÷ 7 = 4
Division as grouping split into groups means there would be in each group.	Use cubes, counters, objects or place value counters to aid understanding. $96 \div 3 = 32$ $96 \div 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 $	of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. 20 $\div$ 5 = ? 5 x ? = 20	Divide 28 into 7 groups. How many are in each group?
Division within arrays	Link division to multiplication by	Draw an array and use lines to split the	Find the inverse of multiplication
	creating an array and thinking about the number sentences that can be created. $15 \div 3 = 5$ $15 \div 5 = 3$ $3 \times 5 = 15$ $5 \times 3 = 15$	array into groups to make multiplication and division sentences.	and division sentences by creating four linking number sentences. $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Division with a remainder A remainder is what is left over after splitting into equal groups. divided by gives equal groups, with remaining.	Use of lollipop sticks to form wholes- squares are made because we are dividing by 4. There are 3 whole squares, with 1 left over.	Children to represent the lollipop sticks pictorially. There are 3 whole squares, with 1 left over.	<ul> <li>13 ÷ 4 - 3 remainder 1</li> <li>Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line.</li> <li>'3 groups of 4, with 1 left over'</li> </ul>
<u>Year 3</u> Short division (no exchange)	Should first be shown using base 10 and shared into groups, to understand the place value.	•••	36 ÷ 3 = 12
In division, we start from the largest place value column. We start from the right.	Use place value counters to divide using the bus stop method alongside Tens Units		2 3 2 4 6
is tens and ones tens divided by is ones divided by is add is e.g. 36 is 3 tens and 6 ones. 3 tens divided by 3 is one ten. 6 ones divided by 3 is 2 ones. One ten add 2 ones is 12.	$3 \qquad 2$ $3 \qquad \bigcirc $		



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Short division (with exchange) e.g. 42 is 4 tens and 2 ones. We can share 3 tens equally with one ten in each group but there is one ten left over. We need to exchange this ten for ten ones. Now we have twelves ones. 12 shared between 3 is 4 ones. In each group there is one ten and 4 ones. 10 add 4 is 14.	Sharing using place value counters. $42 \div 3 = 14$ 000000 10s 1s 0 0 10s 1s 0 0 0 0 0 0 0 0	Represent the place value counters pictorially.	Children to be able to make sense of the place value counters and write calculations to show the process. $42 \div 3$ 42 = 30 + 12 $30 \div 3 = 10$ $12 \div 3 = 4$ 10 + 4 = 14
<u>Year 4 onwards</u> Shortdivision	usingplace value counterstogroup. 615 ÷ 5 1005 105 15 000000	Represent the place value counters pictorially.	Children to the calculation using the short division scaffold. $123$ $5 \cdot 6^{1}1^{1}5$



STRATEGY STEM SENTENCE	CONCRETE	PICTORIAL	ABSTRACT
Long division	1000s         100s         10s         1s         V           1000s         100s         10s         1s         V	Ve can't group 2 thousands into groups of 12 so vill exchange them. We can group 24 hundreds into groups of 12 which leaves with 1 hundred After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12, which eaves 2 tens After exchanging the 2 tens, we have 24 ones. We can group 24 ones onto 2 groups of 12, which leaves no remainder	$12 \begin{vmatrix} 0.2 \\ 2544 \\ 24 \\ 1 \end{vmatrix}$ $12 \begin{vmatrix} 0.2 \\ 2544 \\ 24 \\ 14 \\ 12 \\ 2 \end{vmatrix}$ $12 \begin{vmatrix} 0.2 \\ 2544 \\ 24 \\ 14 \\ 12 \\ 24 \\ 14 \\ 12 \\ 24 \\ 0 \end{vmatrix}$
			Move onto divisions with a remainder. 8       6       r       2         5       4       3       2



STRATEGY	CONCRETE	PICTORIAL	ABSTRACT
STEM SENTENCE			
Children to be able to divide so that there are no remainders, going into the decimal values if needed. Use written division methods in cases			Pupils should be encouraged to note down multiples when dividing by a 2 digit number
where the answer has up to two			<u>14.6</u> 16 21
decimal places.			3 5 5 1 1 . 0
			35 70 105 140 
Concer	tual variation: different w	ays to ask children to solve 615	÷ 5 =
Using the part whole model below, how can you divide 615 by 5 without using short division?	I have £615 and share it equally between 5 bank accounts. How much will be in each account? 615 pupils need to be put into 5 groups. How many will be in each group?	5 615	What is the calculation? What is the answer?
		615 ÷ 5 = ?	100s 10s 1s 000000 000000 000000
		? = 615 ÷ 5	